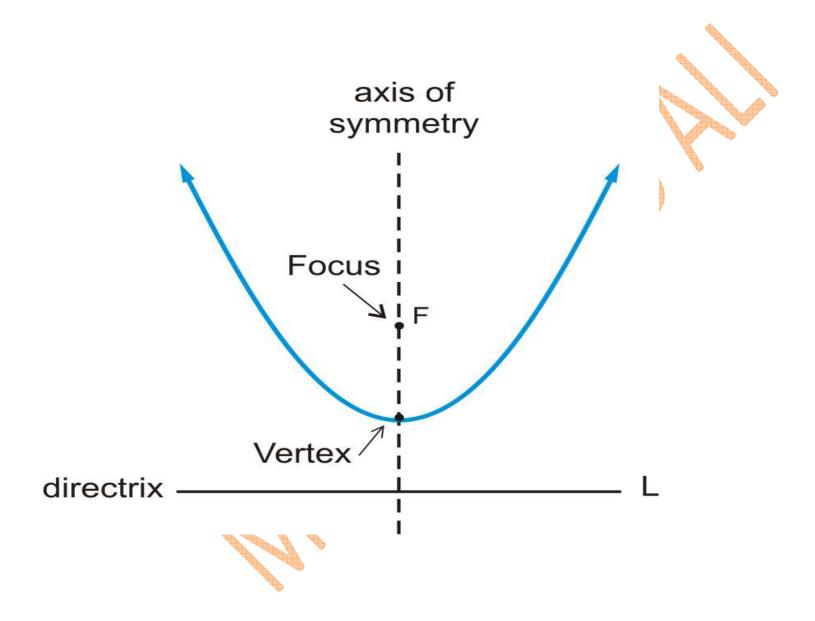


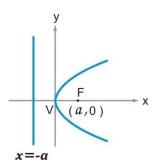
## Chapter 8

# PARABOLAS



## PARABOLA VERTEX AT ORIGIN

(1) Axis along x-axis, open right:



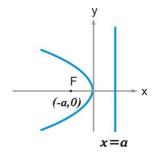
(i) Equation of parabola

$$y^2 = 4ax$$

- (ii) Focus at (a, 0).
- (iii) Equation of directrix

$$x = -a$$

(2) Axis along x-axis, open left:



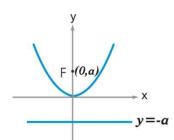
(i) Equation of parabola

$$y^2 = -4ax$$

- (ii) Focus at (-a, 0).
- (iii) Equation of directrix

$$x = a$$

(3) Axis along y-axis, open up:



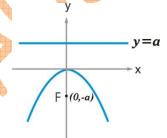
(i) Equation of parabola

$$x^2 = 4ay$$

- (ii) Focus at (0, a).
- (iii) Equation of directrix

$$y = -a$$

(4) Axis along y-axis, open down:



(i) Equation of parabola

$$x^2 = -4ay$$

- (ii) Focus at (0, -a).
- (iii) Equation of directrix

$$y = a$$

#### Formula:

Length of latus rectum = 4a

## **MCQ-1:**

What is the focus of parabola  $x^2 = 12y$ ?

(c) 
$$(0, -3)$$

(d) 
$$(-3,0)$$

**Solution:** 

$$x^2 = 12y$$

There are only two terms, so vertex at origin. The power of y is 1, so axis of parabola is along y-axis.

The coefficient of y is positive (i.e. 12) so it is open up.

Standard equation of parabola

$$x^2 = 4ay$$

$$4a = 12$$

$$a = 3$$

Focus at (0, a) = (0,3)

The answer is (a).

#### MCQ- 2:

What is the focus of parabola  $y^2 + 18x = 0$ ?

(a) 
$$(0, \frac{9}{2})$$

(b) 
$$\left(0, -\frac{9}{2}\right)$$

(c) 
$$(\frac{9}{2}, 0)$$

(b) 
$$\left(0, -\frac{9}{2}\right)$$
 (c)  $\left(\frac{9}{2}, 0\right)$  (d)  $\left(-\frac{9}{2}, 0\right)$ 

Solution:

$$y^2 + 18x = 0$$
$$y^2 = -18x$$

Vertex at origin, axis of parabola is along x-axis and open left because the coefficient of x is negative (i.e. -18).

Standard equation of parabola

$$y^2 = -4ax$$

$$4a = 18$$

$$a = \frac{9}{2}$$

Focus at (-a, 0) =  $(-\frac{9}{2}, 0)$ 

The answer is (d).

### MCQ- 3:

What is the length of latus rectum of parabola  $x^2 = -28y$ ?

- (a) 7
- (b) 28
- (c) 192

**Solution:** 



Standard equation of parabola

$$x^2 = -4ay$$

Length of latus rectum = 4a

$$4a = 28$$

The answer is (b).

## exercise-1

- (1) What are the coordinates of focus of the parabola  $x^2 = -20y$ ?
  - (a) (-20,0) (b) (0,-20)
- (c) (-5,0)
- (d) (0, -5)
- (2) What is the length of the latus rectum of the parabola  $y^2 = -24x$ ?
  - (a) 24
- (b) 6
- (c) 4
- (3) What is the equation of the directrix of the parabola  $x^2 + 32y = 0$ ?
  - (a) y = 32
- (b) y = 8
- (c) x = 8
- (d) x = -8
- (4) What is the equation of the directrix of the parabola  $x^2 = 4ay$ ?
  - (a) y a = 0
- (b) x a = 0
- (c) y + a = 0
- (d) x + a = 0
- (5) e is the eccentricity of a parabola. What is the value of e?
  - (a) 0.5
- (b) 1.5
- (c) 0
- (d) 1

## PARABOLA VERTEX AT ORIGIN

S.No.	Axis of	Open	Equation	Focus	Directrix
	parabola				
1	x-axis	Right	$y^2 = 4ax$	(a, 0)	x = -a
2	x-axis	Left	$y^2 = -4ax$	(-a, 0)	x = a
3	y-axis	Right	$x^2 = 4ay$	(0,a)	y = -a
4	y-axis	Left	$x^2 = -4ay$	(0,-a)	y = a

## PARABOLA VERTEX AT (h, k

S.No.	Axis of	Open	Equation	Focus	Directrix
	parabola				)
1	x-axis	Right	$(y-k)^2 = 4a(x-h)$	(a+h,k)	x = -a + h
2	x-axis	Left	$(y-k)^2 = -4a(x-h)$	(-a+h,k)	x = a + h
3	y-axis	Right	$(x-h)^2 = 4a(y-k)$	(h, a + k)	y = -a + k
4	y-axis	Left	$(x-h)^2 = -4a(y-k)$	(h, -a+k)	y = a + k

## MCQ-4:

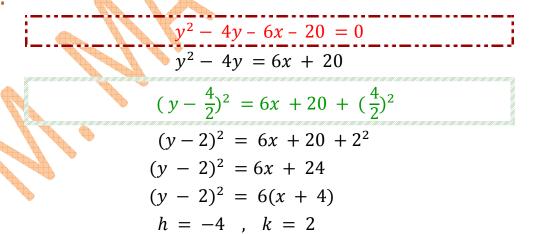
What is the vertex of parabola  $y^2 - 4y - 6x - 20 = 0$ ?

(a) (0, 0)

(b) 
$$(-2, -3)$$
 (c)  $(-4, 2)$ 

(d) (2, -3)

## **Solution:**



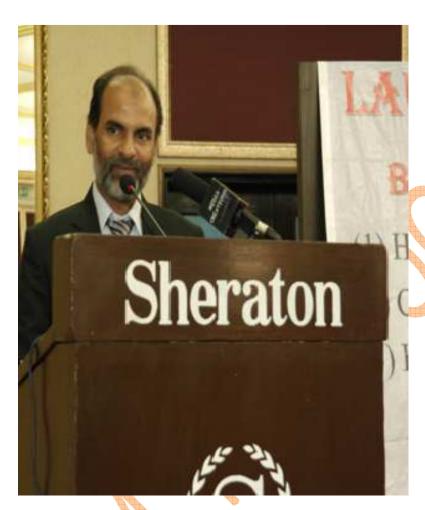
Vertex at (h, k) = (-4, 2)

The answer is (c).

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The answer is (d).

#### EXERCISE-2

(1) What is the vertex of the parabola  $x^2 - 6x - 12y - 51 = 0$ ? [Hint: Find turning point, putting dy/dx = 0] (a) (5, -3) (b) (-3, 5) (c) (3, -5) (d) (-5, 3)

(2) What is the vertex of the parabola  $y^2 + 4y + 4x - 12 = 0$ ? (a) (-2,4) (b) (4,-2) (c) (2,-4) (d) (-2,-4)

(3) What are the coordinates of the vertex of the parabola  $(y+3)^2 = -4(x-7)$ ?

(a) (-7,3) (b) (-3,7) (c) (7,-3) (d) (-1,-3)(4) What are the coordinates of focus of the parabola  $(y-k)^2 = -4a(x-h)$ ?

(4) What are the coordinates of focus of the parabola  $(y-k)^2 = -4a(x-h)^2$ (a) (-a+h,k) (b) (a+h,k) (c) (a+k,h)(d) (-a+h,0)

(5) What are the coordinates of focus of the parabola  $(y-2)^2 = 8(x-3)$ ? (a) (5, 2) (b) (2, 3) (c) (2, 0) (d) (4, 3)

(a) (5, 2) (b) (2, 3) (c) (2, 0) (d) (4, 3)

(6) What are the coordinates of focus of the parabola $(y-5)^2 = -12(x+2)$ ? (a) (-1,5) (b) (-3,5) (c) (-5,5) (d) (2,-2)

(7) What are the coordinates of focus of the parabola  $(x + 6)^2 = 20 (y - 4)$ ? (a) (-6,5) (b) (-1,4) (c) -6,9) (d) (3,2)

(8) What are the coordinates of focus of the parabola  $(x-5)^2 = -8(y-7)$ ?

(a) (5, 5) (b) (5, 7) (c) (-2,7) (d) (3, 7)

(9) What is the equation of the directrix of the parabola  $(x - h)^2 = 4a(y - k)$ ? (a) x + a = h (b) y + a = k (c) y - a = k (d) y = -a

(10) What is the equation of the directrix of the parabola  $(y-k)^2=4a(x-h)$ ?

(a) x = h + a (b) x = h - a (c) y = k - a (d) y = h + a

(11) What is the equation of the directrix of the parabola

 $(x-h)^2 = -4a(y-k)$ ?

(a) y = k + a (b) x = h + a (c) y = k - a (d) x = k - a

(12) What is the equation of the directrix of the parabola

$$(y-2)^2 = 16(x-5)?$$

(a) 
$$x = 5$$

(b) 
$$x = -2$$

(c) 
$$x = 1$$

(d) 
$$y + 2 = 0$$

(13) What is the equation of the directrix of the parabola

$$(x+7)^2 = -4(y-6)?$$

(a) 
$$y = 7$$
 (b)  $y = 5$ 

(b) 
$$v = !$$

(c) 
$$y = 1$$

(d) 
$$y = -8$$

(14) Which is the equation of the directrix of the parabola

$$(x-h)^2 = 4a(y-k)?$$

(a) 
$$x + a = h$$

(b) 
$$y + a = k$$

(c) 
$$y - a = k$$

(d) 
$$y = -$$

## **EQUATION OF PARABOLA**

## **MCQ-7**:

What is the equation of parabola vertex at origin and focus ( -8 , 0 )?

(a) 
$$x^2 = -8y$$

(b) 
$$y^2 = -8x$$
 (c)

(b) 
$$y^2 = -8x$$
 (c)  $x^2 = -32y$  (d)  $y^2 = -32x$ 

(d) 
$$v^2 = -32$$
:

## **Solution:**

Vertex at origin, focus (-8,0)

since ordinate = 0

∴ axis of parabole is along x-axis.

$$abcissa = -8$$

Negative sign shows that parabola is open left and

$$a = 8$$

The equation of parabola is

$$v^2 = -4a^2$$

$$y^2 = -32x$$

The answer is (d).

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$$4a = 16$$
$$a = 4$$

Equation of tangent

$$xx_1 = 2a(y + y_1)$$

$$-4x = 8(y+1)$$

$$-x = 2(y+1)$$

$$x + 2y + 2 = 0$$

The answer is (b).

Note: Tangent at the vertex of the parabola is parallel to x-axis (if axis of parabola is along y-axis) or parallel to y-axis (if axis of parabola is along x-axis). Vertex at (h, k):

i) Equation of tangent, axis of of parabola is along x-axis.

$$x = h$$

ii) Equation of tangent, axis of of parabola is along y-axis.

$$y = k$$

## EXERCISE-4

(1) What is the equation of tangent of the parabola  $y^2 = 32x$  at (3, -5)?

(a) 
$$32x - 5y + 36 = 0$$
 (b)  $16x + 5y + 48 = 0$ 

(b) 
$$16x + 5y + 48 = 0$$

(c) 
$$8x + 5y + 24 = 0$$

(d) 
$$32x + 5y + 96 = 0$$

(2) A tangent is drawn to parabola  $y^2 = 8x$ . What is the equation of tangent at vertex?

(a) 
$$y = 0$$

(b) 
$$x = 0$$

(c) 
$$x = 2$$

(d) 
$$y = -2$$

(3) A tangent is drawn at vertex to the parabola  $(x-8)^2=12(y-3)$ . What is the equation of tangent?

(a) 
$$y = 6$$

(b) 
$$y = 3$$

(b) 
$$y = 3$$
 (c)  $y = -3$  (d)  $x = 8$ 

(d) 
$$x = 3$$

## **CONDITION OF TANGENCY**

S. NO.	EQ. OF PARABOLA	EQ. OF STRAIGHT LINE	CONDITION OF TANGENCY
i	$y^2 = 4ax$	y = mx + c	c = a/m
ii	$x^2 = 4ay$	y = mx + c	$c = -am^2$

## MCQ- 10:

k=?, if the line y=kx-2 is tangent to the parabola  $x^2=8y$ ?

- (a) 1
- (b) 2
- (c) 4
- (d) 8

Solution:



$$a = 2$$

$$y = kx - 2$$

$$m = k , c = -2$$

Condition of tangency

$$c = -am^2$$

$$-2 = -2k^2$$

$$k^2 = 1$$

$$k = \pm 1$$

The answer is (a).

#### EXERCISE-5

- (1) k = ?, if the line y = 3x + k is tangent of the parabola  $y^2 = 36x$ ?
  - (a) 9
- (b) 8
- (c) 6
- (d) 3

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