

**Chapter 15****GRAPHS OF TRIGONOMETRIC FUNCTIONS****PERIODIC FUNCTIONS**

A and B are subsets of real numbers and

$$f : A \rightarrow B.$$

The function  $f$  is said to be periodic function, if

$$f(x + p) = f(x) \quad , \quad \forall x \in A$$

where  $p$  is the smallest number and is called a period.

**PERIODS OF TRIGONOMETRIC FUNCTIONS**

Function	Period	Function	Period
$\sin x$	$2\pi$	$\sin bx$	$2\pi/ b $
$\cos x$	$2\pi$	$\cos bx$	$2\pi/ b $
$\tan x$	$\pi$	$\tan bx$	$\pi/ b $

**MCQ-1 :**

What is the period of  $\cos(-5x)$ ?

- (a) 5      (b) -5      (c)  $2\pi/-5$       (d)  $2\pi/5$

**Solution:**

$$\text{Period of } \cos bx = \frac{2\pi}{|b|}$$

$$\begin{aligned} \therefore \text{period of } \cos(-5x) &= \frac{2\pi}{|-5|} \\ &= 2\pi/5 \end{aligned}$$

The answer is (d).

**MCQ-2 :**

What is the period of  $f(x) = 5 + 3\sin 4x$  ?

- (a)  $4\pi/3$       (b)  $\pi/2$       (c)  $\pi/2 - 5$       (d)  $3\pi/2$

**Solution:**

The period of  $f$  depends on the coefficient of  $4x$ ,  
( angle of sin ) that is 4 and not on 5 and 3.

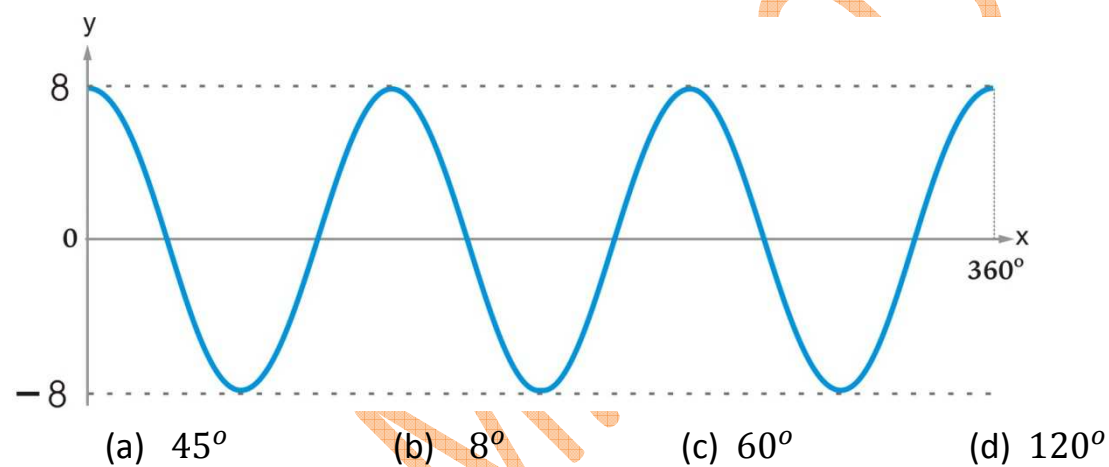
$$\text{Period of } \sin bx = \frac{2\pi}{|b|}$$

$$\text{Period of } f(x) = \frac{2\pi}{4} = \pi/2$$

The answer is (b).

**MCQ- 3:**

The graph of a trigonometric function is given below. What is the period of the function?

**Solution:**

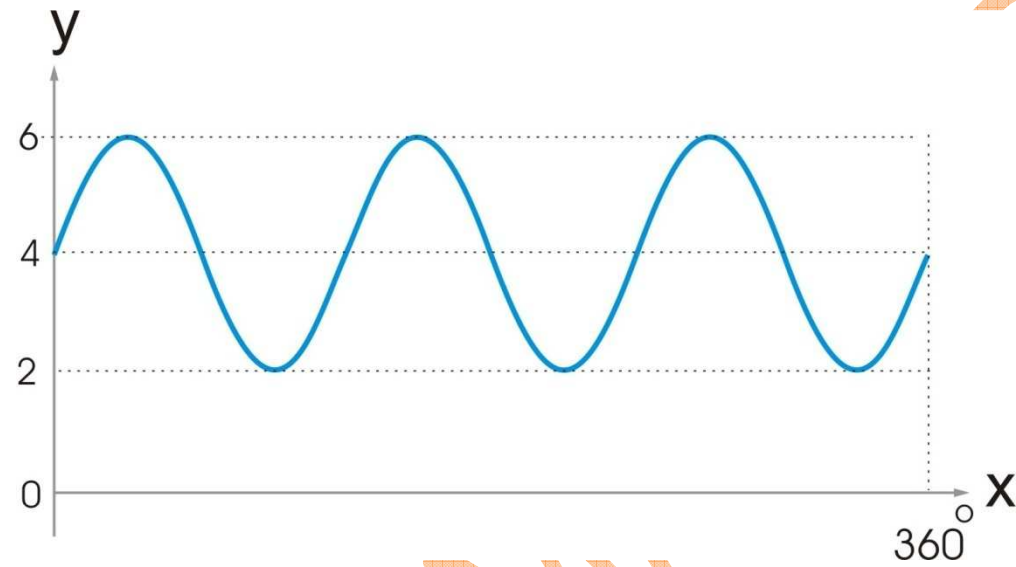
The same shape repeats 3 times between  $0^\circ$  and  $360^\circ$ .

$$\text{Period} = \frac{360^\circ}{3} = 120^\circ$$

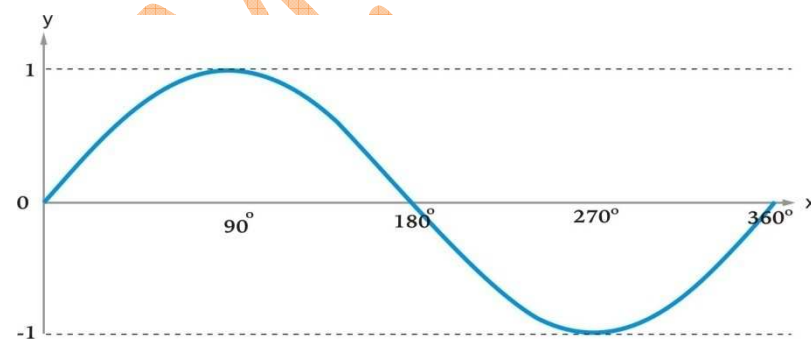
The answer is (d).

**EXERCISE**

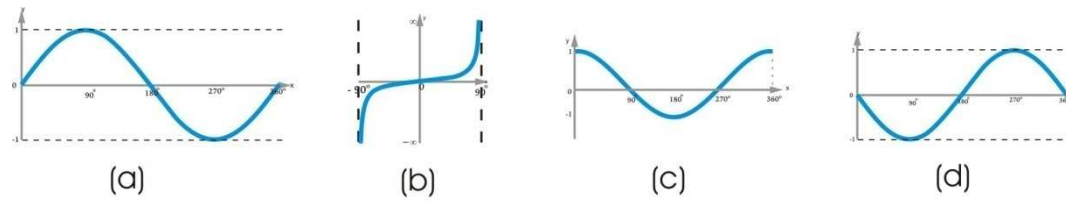
- (1) What is the period of  $3\cos 5x$  ?  
 (a)  $6\pi/5$       (b)  $2\pi/3$       (c)  $2\pi/5$       (d)  $10\pi/3$
- (2) What is the period of  $12 - \tan 4x$  ?  
 (a)  $\pi/4$       (b)  $\pi/12$       (c)  $\pi/2$       (d)  $\pi/2 + 12$
- (3) What is the period of  $6 + 2\cos(-6x)$  ?  
 (a)  $2\pi/3$       (b)  $\pi/3$       (c)  $\pi/6$       (d)  $-\pi$
- (4) What is the period of the following function?



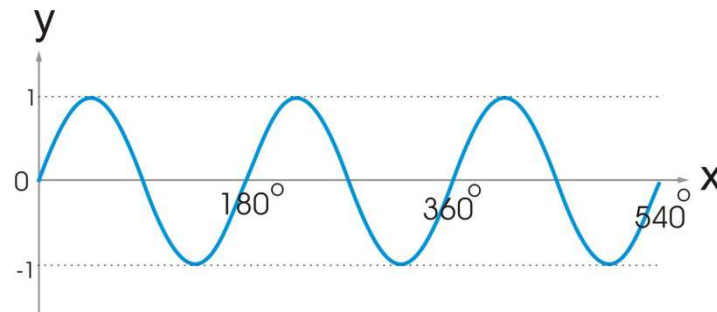
- (a)  $120^\circ$       (b)  $240^\circ$       (c)  $360^\circ$       (d)  $3\pi$
- (5) Following is a graph of a trigonometric function. Identify the function.



- (a)  $\sin x$       (b)  $\cos x$       (c)  $\tan x$       (d)  $\cos^2 x$
- (6) Which graph of the following is the graph of ?



(7) Following is the graph of a trigonometric function. identify the function.



- (a)  $\cos 2x$       (b)  $\sin 2x$       (c)  $\sin 3x$       (d)  $\cos 3x$

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